

Plane Geometry – the study of figures and shapes in two dimensions

Angles

Right angle – a 90° angle that can be indicated by the \perp symbol

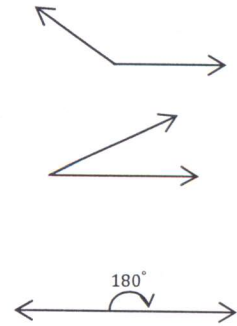
Acute angles – any angle measuring less than 90°

Obtuse angles – any angle measuring more than 90°

Straight angle – any angle measuring 180° in a straight line

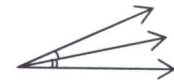
Ex: What are the types and measures of the following angles formed between the hands of a clock:

6 o'clock? 2 o'clock? 3 o'clock? 8 o'clock?

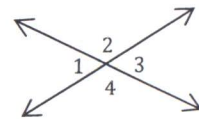


Pairs of Angles

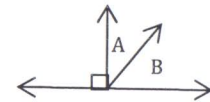
Adjacent Angles – angles that share a common side and common vertex



Vertical angles – when two straight lines intersect the opposite angles are called vertical and are always equal



Complementary – two angles that add up to 90°

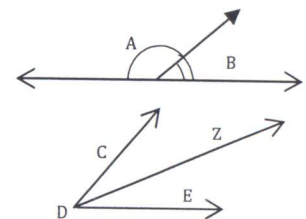


Supplementary – two angles that add up to 180°

Ex: Adjacent angles that form a straight line

Angle bisector – a ray that cuts a single angle into two smaller equal angles

i.e. Ray Z is the angle bisector of angle CDE.



Lines

Straight line – continues in two directions, has infinite number of points and can be named by a single lowercase letter or by any two points on the line.

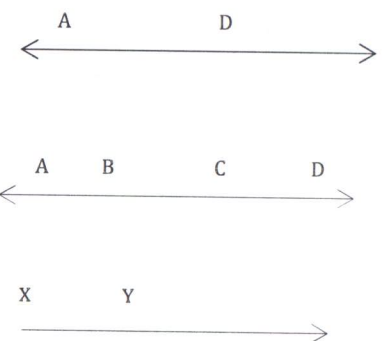
i.e. the line sample line can be named as follows: \overleftrightarrow{AD} or a or b

Line Segment – a part of a line names for its two endpoints

i.e. the sample line segment can be named as follows: \overline{BC}

Ray – has one endpoint and extends to infinite in one direction. It is named by the endpoint and any other point on the ray

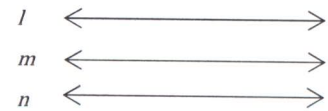
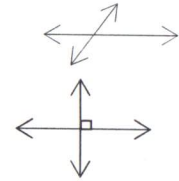
i.e. the sample ray can be named as follows: \overrightarrow{XY}



Intersecting Lines – when two or more lines intersect at a common point

Perpendicular Lines – two line that intersect to form four right angles

Parallel Lines – two or more line that remain the same distance apart and never intersect



Geometric Shapes

Planar

Triangle

Perimeter:

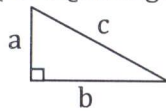
$$P = s_1 + s_2 + s_3$$

Area:

$$A = \frac{1}{2}bh$$

Formulas

Pythagorean Theorem (for right angles):



Equation to find the lengths for each side of a right triangle

$$a^2 + b^2 = c^2$$

The sum of the squares of the legs of a right triangle is equal to the length of the hypotenuse

Quadrilaterals

Square

Perimeter:

$$P = 4s$$

Area:

$$A = s \cdot s = s^2$$

Rectangle:

Perimeter:

$$P = 2(l + w) = 2l + 2w$$

Area

$$A = bh = lw$$

Parallelogram

Perimeter

$$P = 2(l + w) = 2l + 2w$$

Area

$$A = bh$$

Trapezoid

Perimeter

$$P = b_1 + b_2 + s_1 + s_2$$

Area

$$A = \frac{1}{2}h(b_1 + b_2) = h\left(\frac{b_1 + b_2}{2}\right)$$

Circle

Circumference

$$C = \pi d = 2\pi r$$

Area:

$$A = \pi r^2$$

Solids

Cube

Volume:

$$V = s \cdot s \cdot s = s^3$$

Surface Area:

$$SA = s \cdot s \cdot 6 = 6s^2$$

Volume:

$$V = l \cdot w \cdot h$$

Rectangular Solid

Surface Area:

$$SA = 2(l \cdot w) + 2(l \cdot h) + 2(w \cdot h)$$

Volume:

$$V = \pi r^2 h$$

Right Circular Cylinder

Surface Area:

$$SA = 2(\pi r^2) + h(2\pi r)$$